

PROOF OF CIRCLE THEOREMS

ANSWER SHEET

Q1-

Let $\angle PQO = x$ and $\angle RQO = y$

$$\angle PQO = \angle QPO$$

Angles at the base of an isosceles triangle are equal

$$\angle RQO = \angle QRO$$

Angles at the base of an isosceles triangle are equal

$$\angle POQ = 180 - 2x$$

Angles in a triangle add to 180°

$$\angle QOR = 180 - 2y$$

Angles in a triangle add to 180°

$$\angle PQR = x + y$$

$$\angle POR = 360 - (180 - 2x) - (180 - 2y)$$

$$= 360 - 180 + 2x - 180 + 2y$$

$$= 2x + 2y$$

$$= 2(x + y)$$

$$= 2(\angle PQR)$$

Q2-

Let $\angle OPQ = x$ and $\angle OQR = y$

$$\angle OPQ = \angle OQP$$

Angles at the base of an isosceles triangle are equal

$$\angle OQR = \angle ORQ$$

Angles at the base of an isosceles triangle are equal

$$\angle POQ = 180 - 2x$$

Angles in a triangle add to 180°

$$\angle QOR = 180 - 2y$$

Angles in a triangle add to 180°

$$180 - 2x + 180 - 2y = 180$$

$$360 - 2x - 2y = 180$$

$$180 = 2x + 2y$$

$$90 = x + y$$

$$\angle PQR = x + y$$

$$= 90^\circ$$

Q3-

$$POS = x$$

$$PQS = (1/2) x$$

Angle at the circumference is half the angle at the centre

$$PRS = (1/2) x$$

Angle at the circumference is half the angle at the centre

$$PQS = PRS = (1/2) x$$

Q4-

$$\text{Let POR (minor)} = x$$

$$\text{Let POR (major)} = y$$

$$PRS = (1/2) x$$

The angle at the centre is twice the angle at the circumference.

$$PQR = (1/2) y$$

The angle at the centre is twice the angle at the circumference.

$$x + y = 360$$

Angles around a point add to 360°

$$(1/2) x + (1/2) y = 180$$

$$PQR + PRS = 180$$

Q5-

Let $\angle QRT = x$

$\angle ORT = 90^\circ$

Tangent meets radius at 90°

$\angle ORQ = 90 - x$

$\angle UQR = 90^\circ$

Angle in a semicircle is 90°

$\angle QUR = 180 - 90 - (90 - x) = x$

$\angle QPR = x$

Angles from the same points (in the same segment) are equal.

$\angle QPR = \angle QRT = x$
