

Please write clearly in	block capitals.		
Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature			

GCSE MATHEMATICS

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Higher Tier

Paper 2 Calculator

Thursday 7 June 2018

Morning

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- · mathematical instruments.



Instructions

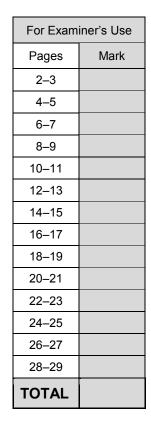
- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
 These must be tagged securely to this answer book.

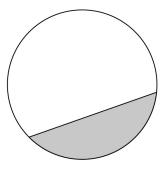
Advice

• In all calculations, show clearly how you work out your answer.



Answer all questions in the spaces provided

1 Here is a circle.



Circle the word that describes the shaded part.

[1 mark]

segment

chord

sector

arc

2 Circle the number that is in standard form.

[1 mark]

$$0.25 \times 10^4$$
 6×10^7 38×10^{-3} $4 \times 10^{\frac{1}{2}}$

$$38 \times 10^{-3}$$

$$4 \times 10^{\frac{1}{2}}$$

3 $y ext{ is } 1\frac{1}{2} ext{ times } x.$

Circle the ratio that is equivalent to y: x

[1 mark]

2:5

5:2

3:2

2:3

Work out 40 as a percentage of 10 Circle your answer.

[1 mark]

4%

25%

300%

400%

Turn over for the next question

4

Match each sequence to its description.One has been done for you.

[4 marks]

1 1 2 3 5 8

Arithmetic progression

1 2 4 8 16 32

Geometric progression

1 2 3 4 5 6

Fibonacci sequence

1 3 6 10 15 21

Triangular numbers

1 4 9 16 25 36

Cube numbers

1 8 27 64 125 216

Square numbers



Population in 2001	Population in 2011	
420 000	480 000	

Liam claims,

"From 2011 to 2021 the population of the city will increase by the same percentage as from 2001 to 2011"

He works out,

population increase from 2001 to 2011 =
$$480\ 000 - 420\ 000$$

= $60\ 000$

Does the population of 540 000 match his claim? You **must** show your working.

Answer

		[3 marks]

Turn over for the next question

1

On three days, Ali throws darts at a target.Here are his results.

	Number of throws	Number of hits	Number of misses
Monday	20	15	5
Tuesday	30	22	8
Wednesday	40	17	23
Total	90	54	36

7	(a)	Work out two different estimates for the probability of Ali hitting the target.	
		Answer and	
7	(b)	Which of your two answers is the better estimate for the probability of Ali hitting target? Give a reason for your answer. Answer	[1 mark]
		Reason	



Theo starts with savings of £18 James starts with no savings.	
Each week from now,	
Theo will save £4.50 and James will save £4	
In how many weeks will Theo and James have savings in the ratio 15:8?	[3 marks]
Answer	



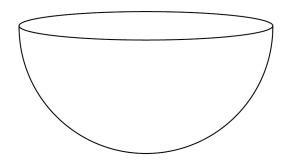
9		The length of each side of a regular pentagon is 8.4 cm to 1 decimal place.	
9	(a)	Complete the error interval for the length of one side.	[2 marks]
		cm < length < cn	1
9	(b)	Complete the error interval for the perimeter.	[1 mark]
		cm perimeter cn	n



10

Volume of a sphere =
$$\frac{4}{3}\pi r^3$$
 where r is the radius

A container is a hemisphere of radius 30 cm



Sand fills the container at a rate of 4000 cm³ per minute.

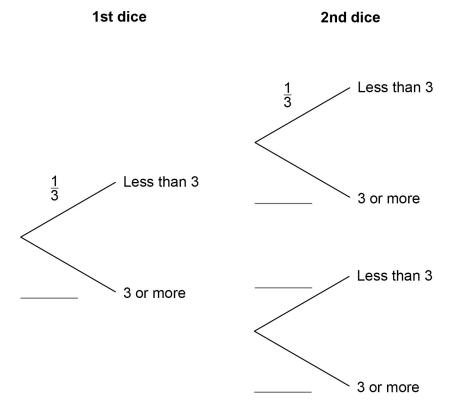
Does it take **less than** a quarter of an hour to fill the container? You **must** show your working.

Answer

[3 marks]

- 11 Two ordinary fair dice are rolled.
- **11 (a)** Complete the tree diagram.

[1 mark]



11 (b) Work out the probability that **both** dice land on a number less than 3

[1 mark]

Answer _____

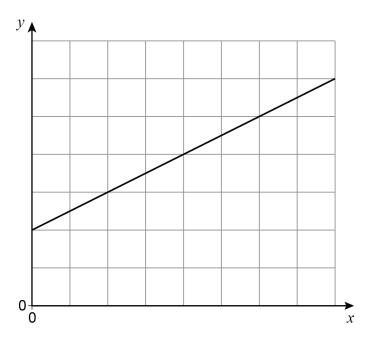
Do not write outside the box	

11	(c)		nn 3 [2 marks]
		Answer	
		Turn over for the next question	

4



12 A straight line is drawn on the centimetre grid.



Fay assumes that the scale is 1 cm represents 1 unit.

12	(a)	Use her assumption to work out the gradient of the line.
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11 marki	Γ1	mark]
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Answer		

12 (b)	In fact, the scale is 1 cm represents 2 units.	Do not write outside the box
	Which statement is correct?	
	Tick one box. [1 mark]	
	The answer to part (a) is too big	
	The answer to part (a) stays the same	
	The answer to part (a) is too small	
	Turn over for the next question	



$\frac{8x^2 - 8}{4x + 4}$ simplifies to the form $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where a and b are integrated as $ax + b$ where $ax +$	gers.

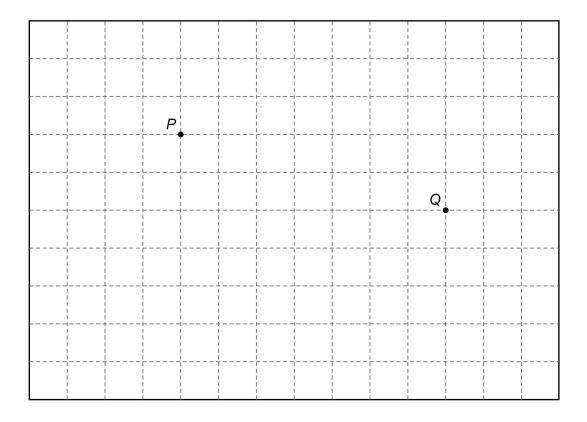


14 The scale drawing represents a garden.

Water from a sprinkler at *P* reaches up to 20 metres from *P*.

Water from a sprinkler at Q reaches up to 25 metres from Q.

Scale: 1 cm represents 5 m



Using a pair of compasses,

show the region that water from **both** sprinklers reaches.

[2 marks]

Turn over for the next question

5



15 100 men and 100 women took a test.

Scores

	Median	Interquartile range	Range
Men	28	7.5	31
Women	30	9	37

Using this data, which statement **must** be true?

Tick **one** box.

[1 mark]

Men had a higher average score than women

Men had more consistent scores than women

A woman had the highest score

A man had the lowest score

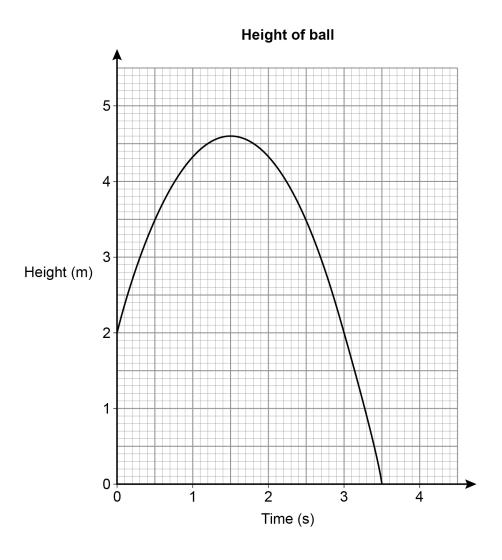


	17		
	Some concrete has volume 3.8 m ³		
)	The density of the concrete is 2400 kg/m ³		
	Work out the mass of the concrete.		[2 marks]
	Answer	₋ kg	
)	The 3.8 m ³ of concrete is made into the shape of a cylinder. The base has radius 0.5 metres.		
	0.5 m		
	Work out the height of the cylinder.		[2 marks]



17 A ball is thrown vertically upwards.

The graph shows the height of the ball above the ground after it is thrown.



17 (a) For how many seconds is the ball at a height of more than 2 metres?

[1 mark]

Answer

17 (b) After how many seconds is the ball at instantaneous rest when it is in the air?

[1 mark]

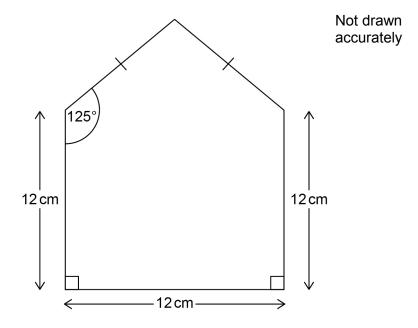
Answer _____ s

	19	
(c)	Work out the average speed of the ball when it is moving downwards.	[2 marks]
	Answer m/s	
	The solution of $3^x = 300$ lies between two consecutive integers. Work out the two integers.	[1 mark]
	Answer and	
	Turn over for the next question	





19	A pentagon is	made from a square	and an isosceles triangle.
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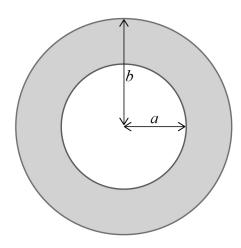
Work out the perimeter of the pentagon.	[4 marks]

Answer _____



cm

20 Here is an inflated swimming ring with dimensions in centimetres.



The volume of the ring, $V \, \mathrm{cm}^3$, is given by

$$V = 0.25\pi^2(b-a)^2(b+a)$$

Work out the volume when a = 20 and b = 30Give your answer to 3 significant figures.

[3 marks]

Answer _____ cm³

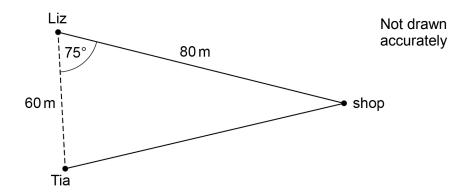
Turn over for the next question

7



Liz and Tia are walking towards a shop along different straight paths.

The diagram shows their positions at 2 pm



21 (a) Assume they walk at the same speed.

Who will arrive at the shop first?

You **must** show your working.

[3 marks]	

Answer			
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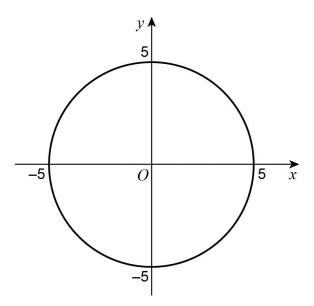
21 (b) In fact, Liz walks at a faster speed than Tia.

How does this affect the answer to part (a)?

[1 mark]



22 A circle, centre O, passes through (5, 0).



What is the equation of the circle? Circle your answer.

[1 mark]

$$x^2 + v^2 = 25$$

$$x^2 + y^2 = 5$$

$$x^2 + y^2 = 10$$

$$x^{2} + y^{2} = 25$$
 $x^{2} + y^{2} = 5$ $x^{2} + y^{2} = 10$ $x^{2} + y^{2} = 100$

Turn over for the next question



		Do not wi
Solids X and Y are similar.		box
X has volume 64 cm ³		
Y has volume 343 cm ³		
The surface area of X is 176 cm ²		
Work out the surface area of Y.		
	[3 marks]	
Answer cr	m^2	



A tank is a cuboid measuring 50 cm by 35 cm by 20 cm All lengths are to the nearest centimetre .	Do not v outside box
A container has a capacity of exactly 34 litres. 1 litre = 1000 cm ³	
Which has the greater capacity? Tick one box.	
Tank Container Cannot tell	
Show working to support your answer. [4 marks]	
Turn over for the next question	



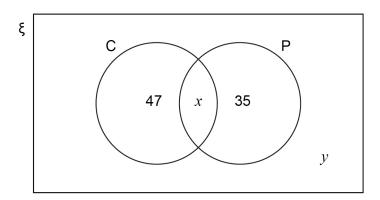


The Venn diagram shows some information about 150 students.

 ξ = 150 students

C = students who study Chemistry

P = students who study Physics



The probability that a Physics student, chosen at random, also studies Chemistry is $\frac{5}{12}$ One of the 150 students is chosen at random.

Work out the probability that the student does **not** study either Chemistry or Physics.

[4 marks]





A line has equation $y = x + 2$ Show that the curve and the line have exactly one point of intersection. Do not use a graphical method. [4 ma	A curve has equation	$y = 4x^2 + 5x + 3$	
Do not use a graphical method.	A line has equation	y = x + 2	
	Show that the curve ar	d the line have exactly one point	of intersection.
	Do not use a graphica	method.	[4 mark

Turn over for the next question

8

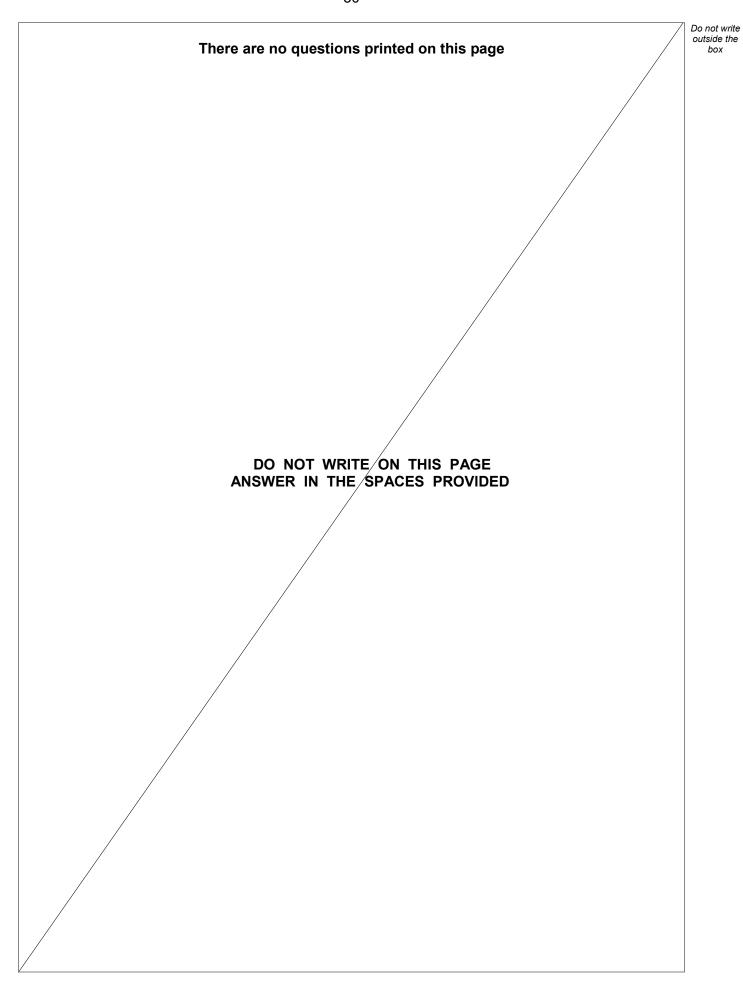


Do not write outside the box 124 Prove algebraically that 2.75 converts to the fraction 27 45 [3 marks]

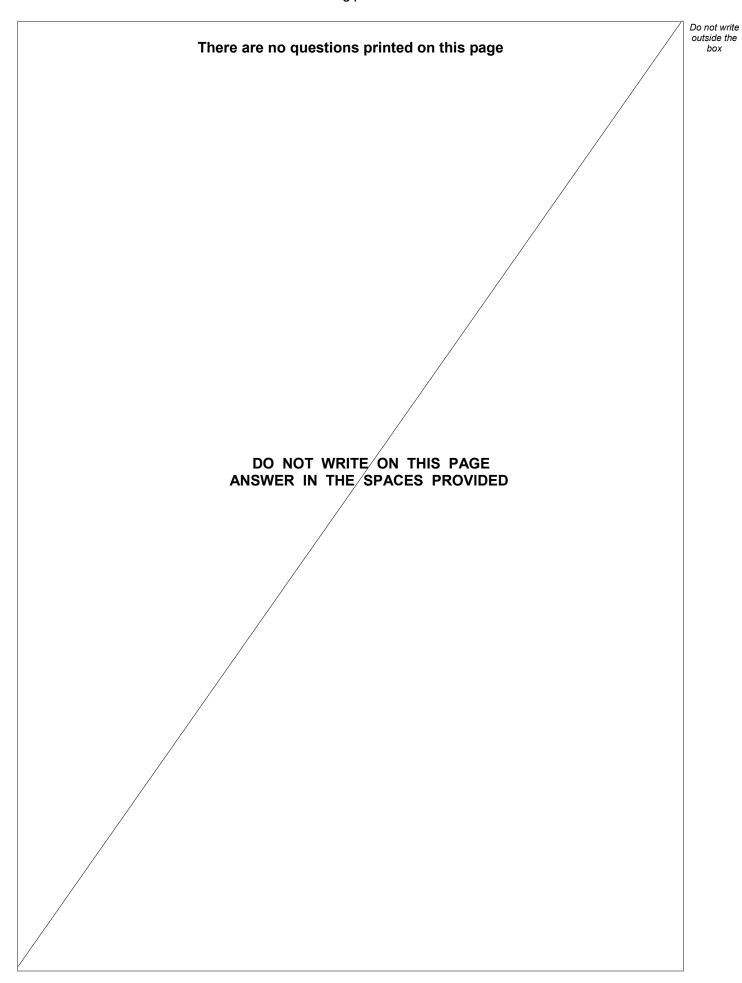


28	f(x) = 5 - x and $g(x) = 3x + 7$	
28 (a)	Simplify $f(2x) + g(x - 1)$	[3 marks]
	Answer	
28 (b)	Solve $g^{-1}(x) = 2x$	[3 marks]
	x =	
	END OF QUESTIONS	

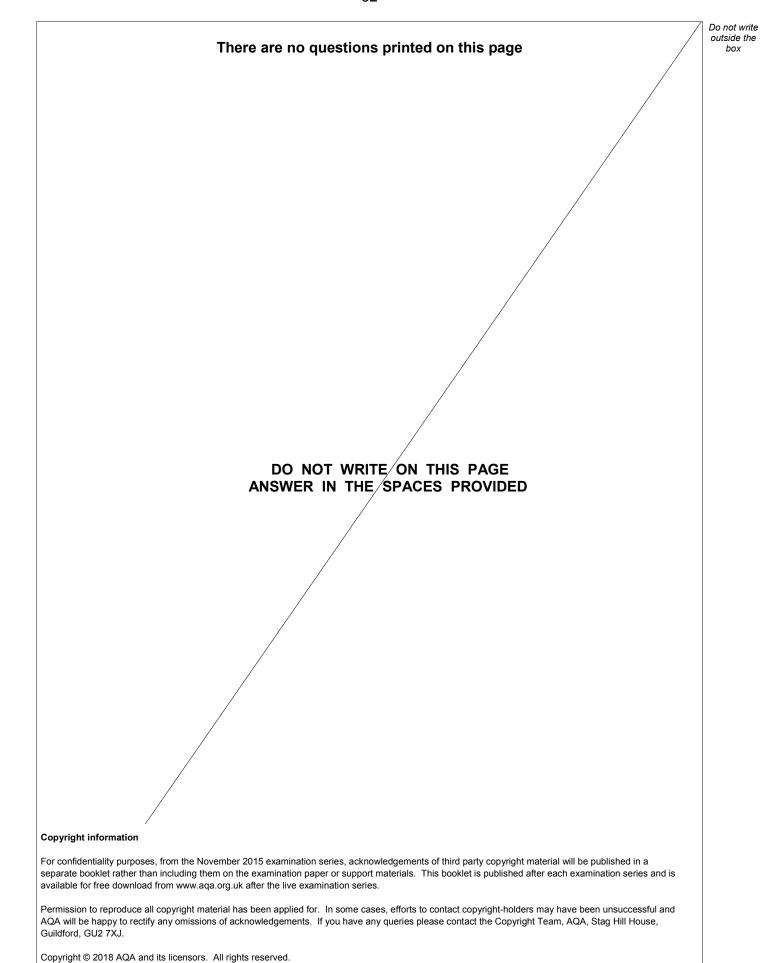












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