

Please write clearly in	block capitals.		
Centre number		Candidate number	
Surname			
Forename(s)			
Candidate signature	,		

GCSE MATHEMATICS

H

Higher Tier

Paper 2 Calculator

Thursday 8 November 2018 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
 These must be tagged securely to this answer book.

Advice

In all calculations, show clearly how you work out your answer.



For Exam	iner's Use
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
TOTAL	

Answer all questions in the spaces provided

1 What does $(A \cap B)$ represent in $P(A \cap B)$? Circle your answer.

[1 mark]

A or B or both

A but not B

not A and not B

A and B

2 P is (4, 9) and Q is (-2, 1) Circle the midpoint of PQ.

[1 mark]

(1, 5)

(3, 4)

(3, 5)

(6, 8)

Which of these is a geometric progression?

Circle your answer.

[1 mark]

1 3 5 7 9

1 3 6 10 15

1 4 9 16 25

1 3 9 27 81



4 The bearing of A from B is 310°

Circle the bearing of *B* from *A*.

[1 mark]

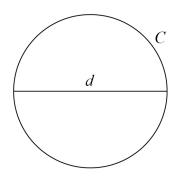
050°

110°

130°

220°

5 A circle has circumference C and diameter d.



C = kd

What **value** does the constant k represent?

[1 mark]

Answer

5



6 Here is some information about 20 trains leaving a station.

Number of minutes late, <i>t</i>	Number of trains	Midpoint	
0 ≤ <i>t</i> < 5	12		
5 ≤ <i>t</i> < 10	7		
10 ≤ <i>t</i> < 15	1		
<i>t</i> ≥ 15	0		

6	(a)	Work out an estimate of the mean number of minutes late.	[3 marks]
		Answer	minutes



6 (b) The station manager looks at the information in more detail.

Number of minutes late, <i>t</i>	Number of trains
0 ≤ <i>t</i> < 2	12
2 ≤ <i>t</i> < 4	0
4 ≤ <i>t</i> < 6	7
6 ≤ <i>t</i> < 8	0
8 ≤ <i>t</i> < 10	0
10 ≤ <i>t</i> < 12	1

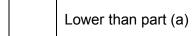
He works out an estimate of the mean using this information.

How does his estimate compare with the answer to part (a)? Tick **one** box.

[1 mark]

Higher than part (a)

Same as part (a)



Turn over for the next question

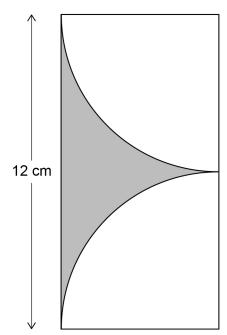
4



7	Work out the values of a and b in the identity		
	5(7x + 8) + 3(2x + b) = ax + 13	[4 marks]	
	a = b =		



8 Two identical quarter circles are cut from a rectangle as shown.



Answer

Not drawn accurately

 cm^2

Work out the shaded area.	[4 marks]

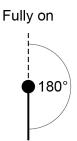
8



9 The diagrams show the position of a tap when off and fully on.

The tap is fully on when the angle of turn is 180°





When fully on, water flows out of the tap at 14 litres per minute.

The rate at which water flows out is in direct proportion to the angle of turn.

The tap is turned 135°



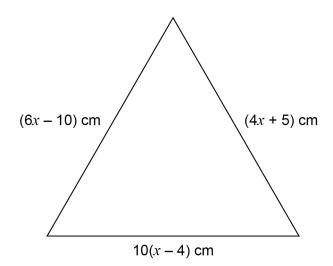
The water flows into a tank with a capacity of 79.8 litres.

Will it take **less than** $7\frac{1}{2}$ minutes to fill the tank?

You **must** show your working.

[4 marks]

10 This triangle is equilateral.



Not drawn accurately

Is the perimeter of the triangle greater than one metre? You **must** show your working.

[5 marks]

9



11	An approximation for the value of π is given by	V
	This approximation for the value of this given by	y

$$4\bigg(1-\frac{22}{57}+\frac{22}{85}-\frac{22}{105}+\frac{22}{117}-\frac{22}{242}\bigg)$$

Use your calculator to	show that this	approximation	is within 0.1	of 3.14

[2 marks]

12 \	Work out	9.12×10^{10}	
12	vvoik out	3.2×10^4	

Give y	our answe	er in star	ndard form.

[2 marks]

Answer _____

Ashraf is going to put boxes into a crate.

The crate is a cuboid measuring 2.5 m by 2 m by 1.2 m Each box is a cube of length 50 cm

He does these calculations.

volume of crate = $2.5 \times 2 \times 1.2$

 $= 6 \, \text{m}^3$

volume of one box = $0.5 \times 0.5 \times 0.5$

 $= 0.125 \,\mathrm{m}^3$

number of boxes = $6 \div 0.125$

= 48

He claims,

"I can put 48 boxes in the crate."

Evaluate Ashraf's method and claim.

[2 marks]

14 The cross section of a prism has n sides.

Circle the expression for the number of edges of the prism.

[1 mark]

2*n*

3n

n + 2

2n + 3

7

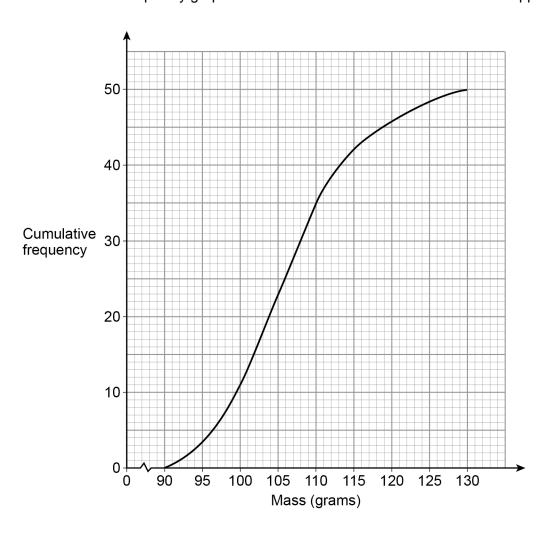


The volume of a medal is 45 cm³ 15 The medal is made from copper and tin. volume of copper: volume of tin = 22:3 The density of copper is $8.96~\mathrm{g/cm}^3$ The density of tin is 7.31 g/cm³ Work out the mass of the medal. [4 marks] Answer grams



Do not write outside the box

16 The cumulative frequency graph shows information about the masses of 50 apples.



16 (a) Use the graph to estimate the median mass of the apples.

[1 mark]

Answer _____ grams

16 (b) Estimate the proportion of the apples that have a mass greater than 115 grams.

[2 marks]

Answer ____

7



17	a is a prime number.		
	b is an even number.		
	$N = a^2 + ab$		
	Circle the correct statement about N .		
	Circle the correct statement about 17.		[1 mark]
			[1.116114]
	could be even or odd	always even	
	always prime	always odd	
18	A bag contains 20 discs.		
	10 are red, 7 are blue and 3 are green.		
40 ()			
18 (a)	Marnie takes a disc at random before putti		
	Nick then takes a disc at random before policy then takes a disc at random.	utting it back in the bag.	
		a rad diga	
	Work out the probability that they all take a	a red disc.	[2 marks]
			[=
	Answer		



40 (1)	AU 00 U		Do not write outside the box
18 (b)	All 20 discs are in the bag.		
	Reggie takes three discs at random, one after the other. After he takes a disc he does not put it back in the bag.		
	Reggie's first disc is blue.		
	Work out the probability that all three discs are different colours.	[3 marks]	
	Answer		
			∐ 6



19

Lunch

Choose one starter and one main course

There are four starters and ten main courses to choose from.

Two of the starters and three of the main courses are suitable for vegans

Two of the state of and three of the main sources are suitable for vegano.	
What percentage of the possible lunches have both courses suitable for vegans	? 3 marks]

Answer

20	n is a positive	integer.
	p	

Prove algebraically that

 $2n^2\left(\frac{3}{n}+n\right)+6n(n^2-1)$ is a cube number.



[3 marks]

21		y is inversely proportional to \sqrt{x} $y = 4$ when $x = 9$	
21	(a)	Work out an equation connecting y and x .	[3 marks]
		Answer	
21	(b)	Work out the value of y when $x = 25$	[2 marks]
		Answer	
		Turn over for the next question	

11



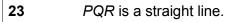
22	Simplify fully	$\frac{x}{}$

$$\frac{x^5-4x^3}{3x-6}$$





Answer _____



$$PQ: QR = 3:1$$

$$\overrightarrow{PQ} = \mathbf{a}$$

Not drawn accurately



Circle the vector \overrightarrow{RQ}

[1 mark]

$$\frac{1}{3}a$$

$$\frac{1}{4}a$$

$$-\frac{1}{2}a$$

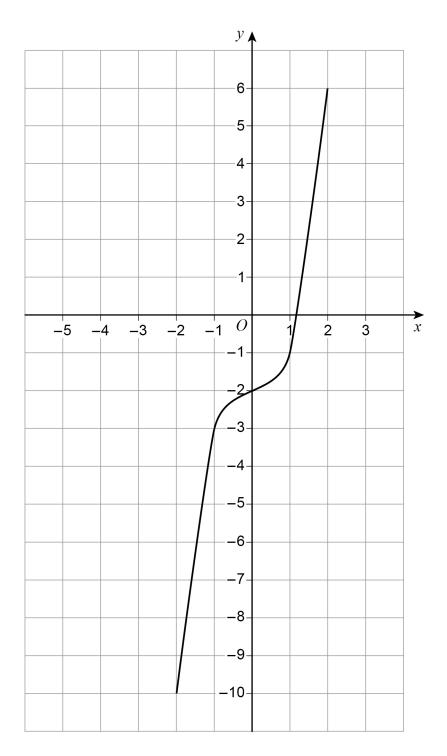
$$-\frac{1}{4}a$$



24 Here is a sketch of y = f(x)

The curve passes through the points

$$(-2, -10)$$
 $(-1, -3)$ $(0, -2)$ $(1, -1)$ $(2, 6)$



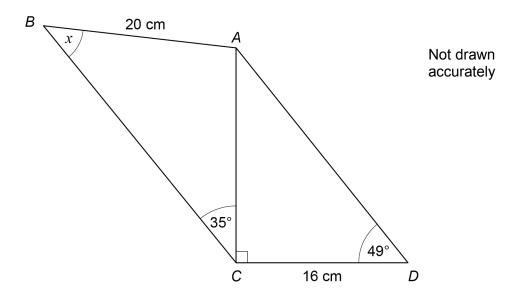
On the grid, sketch the curve y = f(x + 2)

[2 marks]

6



25 ABC and ACD are triangles.



Work out the size of angle x.

	[5 marks]
Answer	degrees



26	$f(x) = \frac{x}{x+2}$	$g(x) = x^2 - 2$
20	x+2	9(3) 30 -

Work out fg(x)

Give your answer in the form $a + bx^n$ where a, b and n are integers.

[3 marks]

Answer _____

The point $\left(3, \frac{1}{64}\right)$ lies on the curve $y = k^x$ where k is a constant.

Show that the point $\left(\frac{1}{2}, \frac{1}{2}\right)$ lies on the curve.

[3 marks]

11



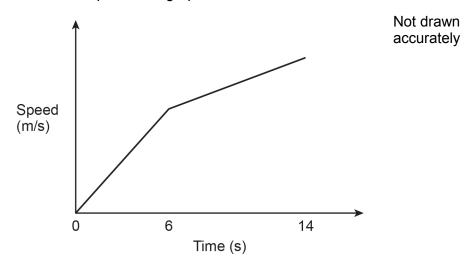
28 Izzy runs an 80-metre race in 14 seconds.

During the first 6 seconds her speed increases at a constant rate.

During the last 8 seconds her speed increases at a different constant rate.

Her speed at 14 seconds is 2 m/s more than her speed at 6 seconds.

Here is a sketch of her speed-time graph.



28 (a) Work out her acceleration during the last 8 seconds.

State the units of your answer.

[2 marks]

Answer			
AIISWEI			

Work out the value of <i>v</i> .	
	[4 marks]
Answer	
END OF QUESTIONS	



