

ANSWER SHEET

Compound and Inverse Functions

Q1

$$\textcircled{1} f(x) = x - 5$$

$$a) f(6)$$

$$f(6) = 6 - 5 \\ = 1$$

$$b) f(4)$$

$$f(4) = 4 - 5 \\ = -1$$

Q2

$$\textcircled{2} g(x) = 2x^2 - 12$$

$$a) g(3) = 2(3)^2 - 12 \\ = 6$$

$$b) g(-3) = 2(-3)^2 - 12 \\ = 6$$

$$c) g(x) = 6$$

$$2x^2 - 12 = 6$$

$$2x^2 = 18$$

$$x^2 = 9$$

$$x = \pm 3$$

Q3

$$\textcircled{3} \quad f(x) = 4x - 6$$

$$a) \quad f(2)$$

$$f(2) = 4(2) - 6$$
$$= 2$$

$$b) \quad f(-2) = 4(-2) - 6$$
$$= -14$$

$$c) \quad f(x) = 2$$

$$4x - 6 = 2$$

$$4x = 8$$

$$x = 2$$

Q4

④

$$f(x) = x^2 - 4$$

$$\begin{aligned} a) \quad f(8) &= (8)^2 - 4 \\ &= 60 \end{aligned}$$

$$\begin{aligned} b) \quad f(-1) &= (-1)^2 - 4 \\ &= -3 \end{aligned}$$

$$c) \quad f^{-1}(x) = 10$$

$$y = x^2 - 4$$

$$x = y^2 - 4$$

$$x + 4 = y^2$$

$$y = \sqrt{x+4}$$

$$\Rightarrow f^{-1}(x) = \sqrt{x+4}$$

$$10 = \sqrt{x+4}$$

$$100 = x + 4$$

$$x = 96$$

Q5

$$(5) \quad f(x) = 2x - 6, \quad g(x) = 3x + 6$$

$$a) \quad f(4) = 2(4) - 6 \\ = 2$$

$$g(2) = 3(2) + 6 \\ = 12$$

b)

$$y = 2x - 6$$

$$x = 2y - 6$$

$$\frac{x+6}{2} = y$$

$$\Rightarrow f^{-1}(y) = \frac{y+6}{2}$$

$$c) \quad 2x - 6 = 3x + 6$$

$$-x = 12$$

$$x = -12$$

Q6

$$\textcircled{6} \quad f(u) = 6u + 1, \quad g(u) = u^2$$

$$a) \quad fg(u) = 6u^2 + 1$$

$$b) \quad gf(u) = (6u + 1)^2$$

$$c) \quad fg(u) = gf(u)$$

$$6u^2 + 1 = (6u + 1)^2$$

$$6u^2 + 1 = (6u + 1)(6u + 1)$$

$$6u^2 + 1 = 36u^2 + 6u + 6u + 1$$

$$6u^2 + 1 = 36u^2 + 12u + 1$$

$$0 = 30u^2 + 12u$$

$$6u(5u + 2) = 0$$

$$u = 0, \quad u = -\frac{2}{5}$$

Q7

$$\textcircled{7} \quad f(u) = u^2 + 2, \quad g(u) = u + 4$$

a) $g^{-1}(u)$

$$y = u + 4$$

$$u = y + 4$$

$$y = u - 4$$

b) $y = u^2 + 2$

$$u = y^2 + 2$$

$$y = \sqrt{u - 2}$$

c) $\sqrt{u - 2} = u - 4$

$$u - 2 = (u - 4)^2$$

$$u - 2 = (u - 4)(u - 4)$$

$$u - 2 = u^2 - 4u - 4u + 16$$

$$u - 2 = u^2 - 8u + 16$$

$$0 = u^2 - 9u + 18$$

$$0 = (u - 3)(u - 6)$$

$$\Rightarrow u = 3 \text{ OR } u = 6$$

Q8

$$\textcircled{2} \quad f(x) = x^2 - 16$$

$$a) \quad f(x-3)$$

$$\begin{aligned} f(x-3) &= (x-3)^2 - 16 \\ &= (x-3)(x-3) - 16 \\ &= x^2 - 3x - 3x + 9 - 16 \\ &= x^2 - 6x - 7 \end{aligned}$$

$$b) \quad f(x-3) = 0$$

$$x^2 - 6x - 7 = 0$$

$$x^2 - 7x + x - 7 = 0$$

$$x(x-7) + 1(x-7) = 0$$

$$(x+1)(x-7) = 0$$

$$x = -1 \quad \text{OR} \quad x = 7$$

Q9

$$\textcircled{a} \quad f(x) = 4x - 2$$

$$a) \quad y = 4x - 2$$

$$x = \frac{y + 2}{4}$$

$$\frac{x + 2}{4} = y$$

$$\Rightarrow f^{-1}(y) = \frac{y + 2}{4}$$

$$b) \quad g(x) = mx^2$$

$$\therefore f(g(2)) = 14$$

$$g(2) = 4m$$

$$\text{For } f(g(2)),$$

$$\text{since } g(2) = 4m$$

$$f(4m) = 4(4m) - 2 \\ = 16m - 2$$

$$\therefore (f(g(2)) = 14)$$

$$16m - 2 = 14$$

$$16m = 16$$

$$m = 1$$